



## Designing Tasks for CAS/DGS Classrooms

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## DESIGNING TASKS FOR CAS/DGS CLASSROOMS

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Fakulteta za *matematiko in fiziko*



- Industrial Age → Information Age
- Major influence on educational systems
  - Some interesting data: Project Tomorrow (<http://www.tomorrow.org>)
    - Creating our Future: Students Speak Up about their Vision for 21st Century Learning, Project Tomorrow (2010)
- Informatization
  - Of the teaching process
  - Of everyday life:
    - Students (learners)
      - "Net (digital) natives"
    - your students are probably **not** DN yet, but ...
- Requirement for individualization

- We live in a society, where everything is individualized and personalized:
  - we personalize our cell phones with ringtones, wallpapers, and skins
  - Experience in buying a bicycle ...
- What about the resources used for teaching?

- Not all students are able to learn successfully
  - at the same pace
  - with the same approach,
  - in the same environment,
  - following the same path,
  - in the same style and manner.
- Research confirms that every individual assimilates information according to their own unique learning style, need, and interest.
- Learning styles vary.

- Challenge for the teacher:
  - Concretize educational content and adapt it to the interests and capability of students
- And of course
  - With appropriate usage of technology in mind

- Substantial research done on appropriate usage
- If we want very short summary
- Two sentences from
  - [Teaching Matters: A handbook for UTS academic staff](#), University of Technology, Sydney, Institute for Interactive Media and Learning,
- “New technologies should be used in the most appropriate way to provide a quality learning experience for students. “

“The **most effective** kind of learning experience is determined not by the technology available, but by considering what is **most appropriate** for the students, the subject and the learning objectives and then selecting **the most appropriate technology** to use, be it a book, an online discussion, a multimedia simulation, or a workplace experience.”

- Appropriate usage of technology
- Personalitization and customization



- Different role of teachers
- Different ways to prepare the resources

**ARE THE RESOURCES PREPARED  
ACCORDING TO THESE NEW  
REQUIREMENTS THE TEACHER IS  
FACING?**

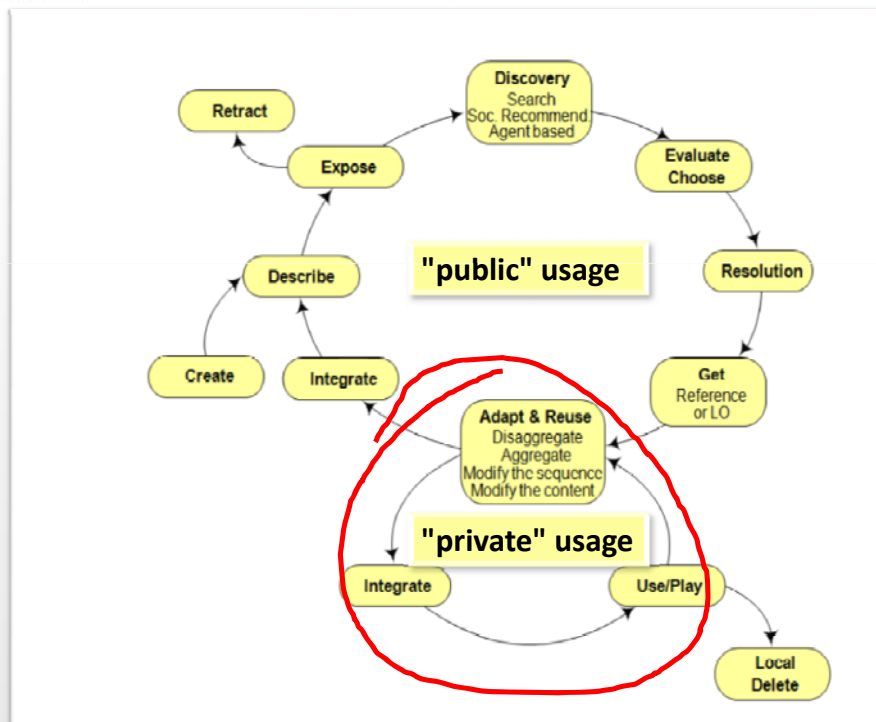
- When designing and evaluating CAS/DGS tasks, we should envision the whole process of their design, usage and modification. A view on a specific task namely changes according to a specific didactical situation.
- CAME06 (Belgrade 2009)
  - **Margot Berger: Designing Tasks For CAS Classrooms: Challenges And Opportunities For Teachers And Researchers**
  - She used semiotic framework to deconstruct CAS-based task into three key components.
  - To illustrate how framework illuminates aspects of the task design that may promote or hinder mathematical activity.

- *Determine the values of  $x$  for which the quadratic approximation  $p(x)$  found previously is accurate to  $f(x)$  within 0.1. [Hint: Graph the functions,  $f(x) = \cos x$ ,  $p(x)$ ,  $y_1 = \cos x + 0.1$  and  $y_2 = \cos x - 0.1$  on a common screen.]*
- Task may have better achieved its intended aim - regarding notion of an approximating polynomial - had I explicitly suggested a reasonable window.
- In pedagogical contexts where students are better rehearsed in using CAS, such an explicit instruction may not be necessary.
- This example illustrates how a small change in the task design may have powerful implications for the quality of the learning that may result.

- Specific pedagogical situation, particular group of students
- With another group – different analysis, different epistemic value, different ...
- Instead of **speculating** the precise **ratio** of both the procedural and the conceptual approach to make the task **suitable for all** students:
- Tasks should be designed in such a way that this **ratio** can easily be **adapted** to the **needs of the user**, be it a teacher or a student.

- But ...
  - Different class, different situation ...
  - How often do you use the same resource twice without modifications?
- So we often wear different hats
  - developer of the resource
  - user of the resource
- Even if we use resources by ourselves

# The "life cycle" of a resource



Frans Van Assche, Riina Vuorikari, (2006). A Framework for Quality of Learning Resources. In U. Ehlers & J.M. Pawlowski (eds.), *European Handbook for Quality and Standardization in E-Learning*

# Usage of resource

- Majority (up to 95% or even more) of the use of e-resources
  - not by authors themselves
  - (unpublished EdReNe internal study)
- Hwang, D., EDUNET: The Core of Korea's Knowledge Bank, 2<sup>nd</sup> Strategic meeting EdReNe, Lisbon, June 2008
  - Resources teacher knows to be adaptable are more accepted and used
    - Although they are mostly not changed



- One size fits all
  - ~~The resource suitable for all students~~
  - Adaptation of the resource according to particular learner's needs
- Choice of tools
  - ~~perfect math environment, CAS with "all functions"~~
  - "cooperation of tools"
- Interactivity
  - What, why, when, how, ...

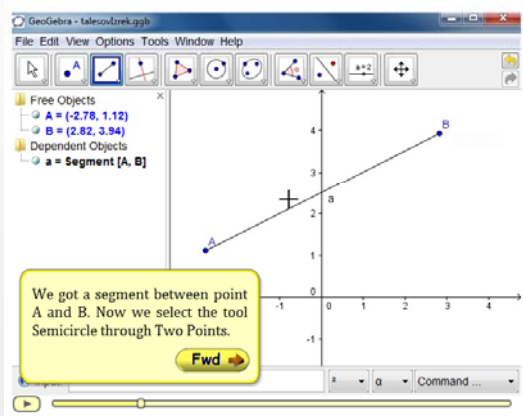
## “One size fits all” syndrome

- To provide instructions, to design a CAS task “suitable for all students”
- Why not:
  - “sub-hints”, proper navigation, “dynamic help”
  - exploiting possibilities technology gives
    - Lack of cooperation with CS experts (GUI ...)
- And again
  - Expandable / changeable by “actual providers to learners”: teachers

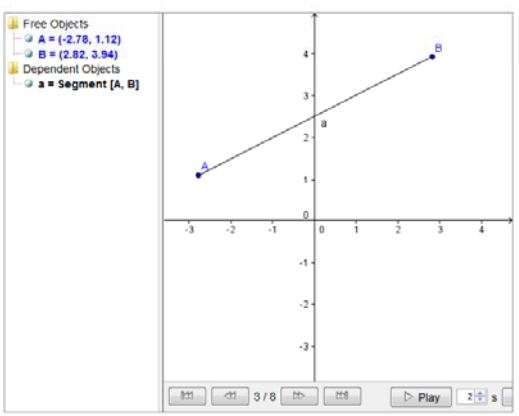
- ◆ Problems in design of CAS tasks could be seen in a different light if another tool was to be used.
  - ◆ Often in just a part of task completion
- ◆ Overcame the wish to stay within the same environment, the same program
- ◆ amazing tricks can be seen, features exploited in unusual ways ... done in Derive, GeoGebra, Mathematica ... or tricky instructions are provided
  - ◆ to stick with the same tool at any cost

- ◆ Part of the teaching process is also to teach students how to choose the most appropriate tools for the task
  - ◆ and “NetGeneration” has no (or significantly less) problems with multitasking
- ◆ We should use different tools
  - ◆ One of the major aspect of the learning process
    - ◆ To choose the most appropriate tool
- ◆ Tools should “cooperate”

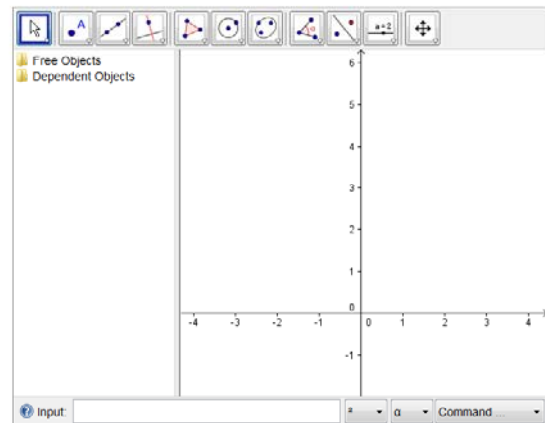
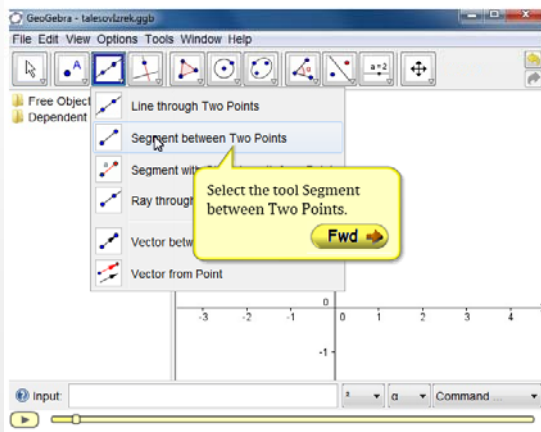
- Task – produce a resource explaining Thales' theorem
- Different models
  - Agreement: web page
  - GeoGebra as a tool
- Which one to choose?
- Which one is the most suitable?



### Thales' Theorem



## Thales' Theorem



# Construction steps with list steps/ GGA

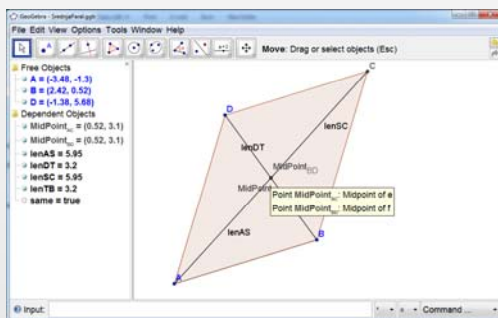
## Thales' Theorem

No.	Name	Definition	Value
1	Point A		$A = (-2.78, 1.12)$
2	Point B		$B = (2.82, 3.94)$
3	Segment a	Segment [A, B]	$a = 6.27$
4	Arc c	Semicircle through B and A	$c = 9.85$
5	Point C	Point on c	$C = (2.63, 0.79)$
6	Triangle poly1	Polygon A, B, C	$poly1 = 8.54$
6	Segment c1	Segment [A, B] of Triangle poly1	$c_1 = 6.27$
6	Segment a1	Segment [B, C] of Triangle poly1	$a_1 = 3.15$
6	Segment b	Segment [C, A] of Triangle poly1	$b = 5.42$

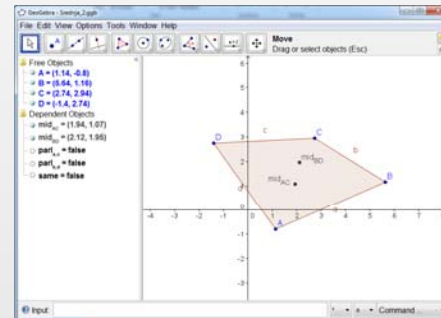
- Cabri Geometre or C. a. R. instead of GeoGebra
- Group of teachers polled
- No "first place"
- Votes dispersed among all possibilities
- Is it really wise for the author to make a choice which **can not be changed**?

- Not just amplifying the "classical approach"
  - To easily demonstrate more cases than in "paper and pencil environment"
- New approaches are needed
- Consideration during design process
- Example:
  - Midpoints of diagonals of the parallelogram

- Middlepoints of diagonals of parallelogram are the same point
  - Just showcase, same approach as in paper/pencil environment

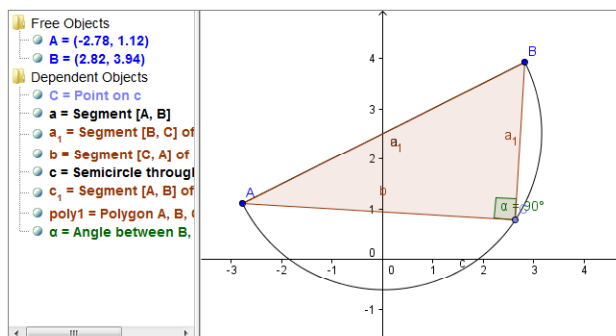


- If middlepoints of diagonals of convex quadrilateral are the same point → quadrilateral is parallelogram
  - "added value"



## Thales' Theorem

Move the point C and watch if the angle between AC and BC changes.

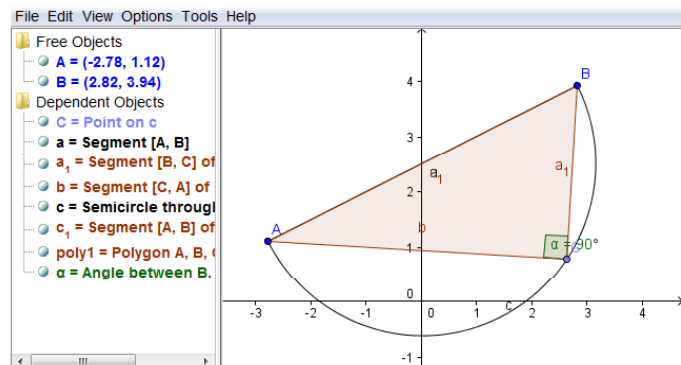


The point C is a point on arc C. We can move the point C only along the arc c.

Download [ggb file](#)

## Thales' Theorem

Move the point C and watch if the angle between AC and BC changes.



The point C is a point on arc C. We can move the point C only along the arc c.

Difference?

- is the one who must adapt the resource to concrete teaching situation and to a particular student
- So the teacher takes from the various resources and reorganizes and adapts author's ideas and models in his/her own way

- Author creates the resources for an ideal situation, teacher teaches in “real world”
- Teacher should gain control over the resource
- Author should merely be an initiator of the resource in various forms
  - Teacher is the one who upgrades the idea, adapts it to a certain pedagogical situation, his/her beliefs, ...
  - Teacher has the possibility to:
    - Adapt
    - Change
    - (Re)combine

- NAUK (advice / study)
  - **N**Apredne **U**čne **K**ocke – NAUK
  - Advanced Learning Blocks





**nauk.si**  
Napredne učne kocke

**Opozorilo:** Aplikacija za izdelavo gradiv se začasno nahaja na [dev.nauk.si](http://dev.nauk.si)  
Tam lahko pripravite tudi gradiva za natečaje.



Matematika



Fizika



Logika



Računalništvo

Zbirke gradiv	Zbirke iz matematike	Zbirke iz fizike	Zanimivo
<ul style="list-style-type: none"> <li>• SIQ</li> <li>• Izvirna znanja</li> </ul>	<ul style="list-style-type: none"> <li>• E-um</li> <li>• Matematika - vaje</li> </ul>	<ul style="list-style-type: none"> <li>• Fideji</li> <li>• Fizik.si</li> </ul>	<ul style="list-style-type: none"> <li>• Wolfram Demonstrations</li> <li>• Puzzlers Paradise</li> </ul>

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# E-LEARNING CONTENT SHOULD BE EASILY ADAPTABLE BY THE TEACHERS

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# Gracias por su atención!